

Strength and ductility of external steel collared concrete columns under compressive loading

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Abstract: Many studies have revealed that one way to improve the performance of concrete columns is by providing confinement. Recently, external confining methods have drawn interest of researchers due to its main advantage for retrofitting purpose of existing members. Steel jacketing methods have long been proposed by several studies for externally retrofitting circular concrete columns. On the other hand, the lack of research has been found in addressing its impacts on the rectangular and square concrete sections. This paper discusses the experimental results and behavior of concrete columns under concentric static axial loading. Nine column specimens were cast and tested to observe their behaviors. A control specimen (CS01) was cast without confinement, while another one (CS03a) was provided with internal stirrups to conform the seismic requirements of building code. The other seven specimens were retrofitted with a set of L-shaped steel collars. Specimens S04a and S04b have both traditional internal stirrups and external L-shaped steel collars. These specimens were intended to simulate the retrofitting work of existing RC columns. The other specimens (S04, S04c, S04d, S04e, and S04f) used various collar configurations to examine the impact of this new retrofitting method. The results have shown significant improvement in both strength and ductility of square concrete column confined externally by L-shaped steel collars.

Keywords: compressive strength, ductility, external confinement, retrofit, square concrete columns, steel collars.

1. Introduction

Concrete under compression suffers tensile stress or strain due to lateral expansion [1-2]. One of the important issues is the brittle failure of concrete due to this axial compressive loading. When an unconfined concrete member is in progressive axial compression, it will fail in a brittle manner. However, this condition will not occur when a concrete member is well confined. The higher the confining degree is provided, the later the concrete member will fail beyond the post-peak response. This improved behavior is certainly needed to significantly delay the failure of structural components during the severe earthquake strike. The ductile behavior is strictly required by the latest building codes which have implemented the modern seismic

design concept of earthquake-resistant RC buildings [3-6].

The use of traditional transverse reinforcement has been well recognized to improve the strength and ductility of concrete members considerably [7-11]. Many efforts have been made to propose analytical model of the improved peak strength as well as the resulting axial stress-strain relationship of confined RC columns [12-19]. In addition, many studies have also been conducted to experimentally investigate the benefits of this confinement [8,20]. The scope of those studies has included vast variety of parameters. Concrete columns with circular, rectangular, and square sections have been covered. The specimens have been tested by axial as well as combined axial and bending load in monotonic and cyclic patterns. Both normal and high strength concrete have been addressed [11,21-23]. Some variables have been concluded to affect the confined concrete behavior, such as the plain concrete compressive strength, yield strength of confining reinforcement, volumetric ratio of confinement steel to concrete core, tie spacing and resulting tie configuration, and the amount of longitudinal steel around the core perimeter. The improved stress-strain relationship of confined concrete is characterized by the increment of compressive strength, flatter post-peak

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descending branch of the curve, and increment of ultimate compressive strain [24].

Besides the conventional confinement studies, many other studies have been conducted to investigate the advantages of external confinement methods [25-32]. Such external confinement approaches are essential to develop due to high demands on concrete columns retrofits. The contact behavior between concrete and external confinement elements, distribution of confining stress in 3D space, and the resulting failure mechanisms, which can be totally different to those of conventional stirrups, are promising areas for research in the external confinement approaches. Early studies of this approach have been proven to be successful in dealing with circular concrete columns. On the other hand, providing effective confining stress by external retrofit for rectangular and square columns is not a simple task. As in the case of internal confinement, the confining stress in the sectional shapes, is not uniform due to the stress concentration in the corners. Relatively fewer experimental and analytical studies are found to investigate this behavior [33-35]. Recently, external confinement method to strengthen square RC columns by using hollow-square steel section collars has been proposed and proven to be successful in improving the strength and ductility of the confined columns. To further investigate the effectiveness of such approach, an external confining method that utilizes light L-shaped steel section collars is studied for its capability as an alternative retrofit for square concrete columns.

2. Experimental setup

Nine columns specimens were built and tested under monotonic concentric compressive loading. Two control specimens, CS01 and CS03a, were built without any confinement and with internal stirrups, respectively, to conform the seismic requirement of the code [3]. The other seven were externally confined by a set of L-shaped steel section collars. Two of those seven specimens (S04a and S04b) were initially confined with traditional internal stirrups. A set of L-shaped steel collars were then installed externally in order to observe the combined effect of both confinements. The observed behaviors can be used to confirm whether the proposed retrofitting method can be used to strengthen existing RC columns. The effect of external confinement alone was represented by Specimen S04. The rest of the specimens (S04, S04c, S04d, S04e, and S04f) are varied in terms of the application of the L-shaped steel section collars to study the extended use of the proposed approach. The strength and ductility enhancements of con-

crete columns retrofitted by external L-shaped steel section collars were the main objective of the study. The sectional dimensions of the L-shaped steel section collars were 40 mm × 40 mm × 4 mm (L40.40.4). It will be abbreviated as L40 in the next sections of the paper. The external confinement was implemented to the column specimens by fastening the structural bolts at the four corners of a set of L-shaped steel section collar assemblage. The illustration of the assembled perspective view of a typical specimen is shown in Fig. 1.

The dimension of the specimen was 600 mm in height with square cross section (200 mm × 200 mm). Heavy confinement was installed in both 100-mm bottom and top ends of the specimens. Thus, no damage was expected in these non-test regions. Various configurations of external confinements were installed in the 400-mm mid-test regions, except for control specimens, CS01 and CS03a, with internal confinement only. In order to determine the gage length, a set of two rods was installed within the test regions protruding out from each face of the column specimens. Totally four LVDTs (Linear Variable Differential Transducers), one on each side of the specimens, were attached to the rods to measure the axial strain during the test.

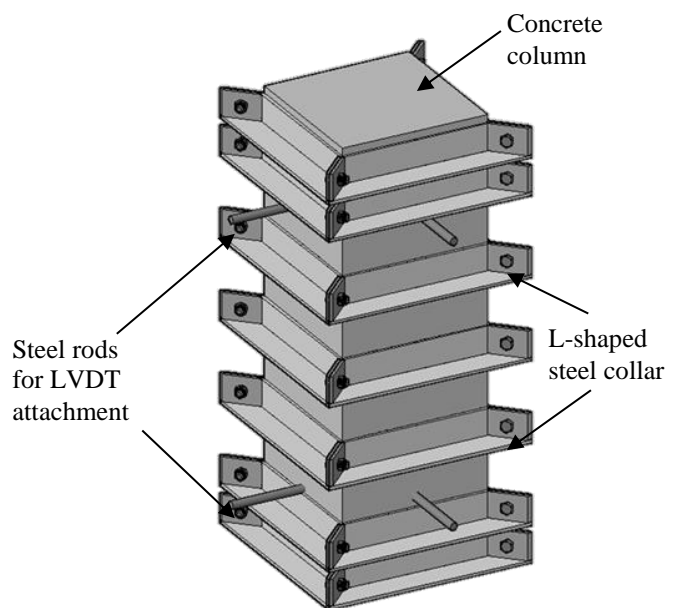


Fig. 1 – Assembled typical specimen

3. Test specimens

Illustrations of the specimens described previously are presented here. The longitudinal sections of the internal confinement can be seen in Fig. 2. The two control specimens, CS01 and CS03a, are shown in Fig. 2. Figure 2(a) represents specimens with no internal stirrups in the middle test region. To fulfill the code [3] requirement for seismic confinement, Specimen CS03a was built with D10-

50 stirrups (Fig. 2(b)). The volumetric ratio was found to be 2.36 percent. The volumetric ratio is defined as the volume of the confinement steel with respect to the volume of column, obtained by multiplying the gross cross-sectional area and the spacing of confining elements. Figures 2(c) and (d) depict the internal stirrups of Specimens S04a and S04b, respectively. Specimen S04a was built such that the location of the internal and external confinements coincided with each other (volumetric ratio of 1.48 percent). Specimen S04b was modified from S04a such that the internal confinement could be placed exactly at the mid-spacing of the external L-shaped steel section collars. These two column specimens were intended to study and anticipate the influence of the two possible extreme locations of the external steel collars with regards to the location of the internal confinement in the existing columns. These two efforts are intended to consider the pos-

sible application of the proposed retrofitting method on existing RC columns in actual buildings.

The external confinement arrangements of the specimens are presented in Figs. 3 and 4. Specimens S04, S04a, and S04b are externally confined with L-shaped steel collars at 80 mm spacing without any web stiffeners or bolts (see Fig. 3(a)). The volumetric ratio of the external confinement is 9.60 percent. Figures 3(b) and (c) show the external confinement arrangements of Specimens S04c and S04d, respectively. The steel collars are strengthened with additional one and two web stiffeners made from 6-mm thick steel plates for Specimens S04c and S04d, respectively. Figures 4(a) and (b) depict the external confinement arrangements of Specimens S04e and S04f, respectively. The contacts of steel collars to the concrete are strengthened with one and two additional bolts for Specimens S04e and S04f, respectively. The cross sections of the specimens are given

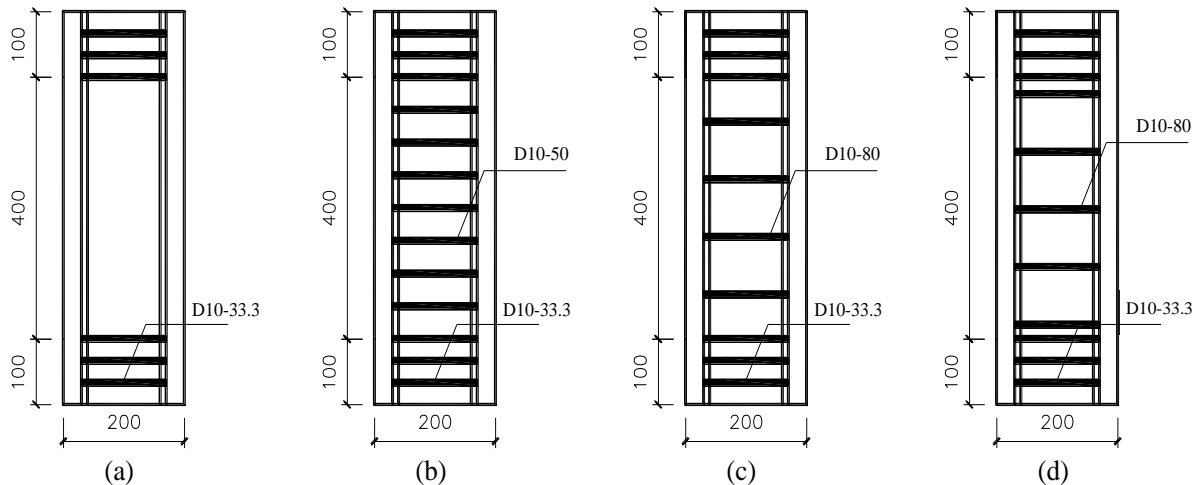


Fig. 2 – Longitudinal sections of internal confinement arrangements of specimens: (a) CS01, S04, S04c, S04d, S04e, S04f; (b) CS03a; (c) S04a; (d) S04b

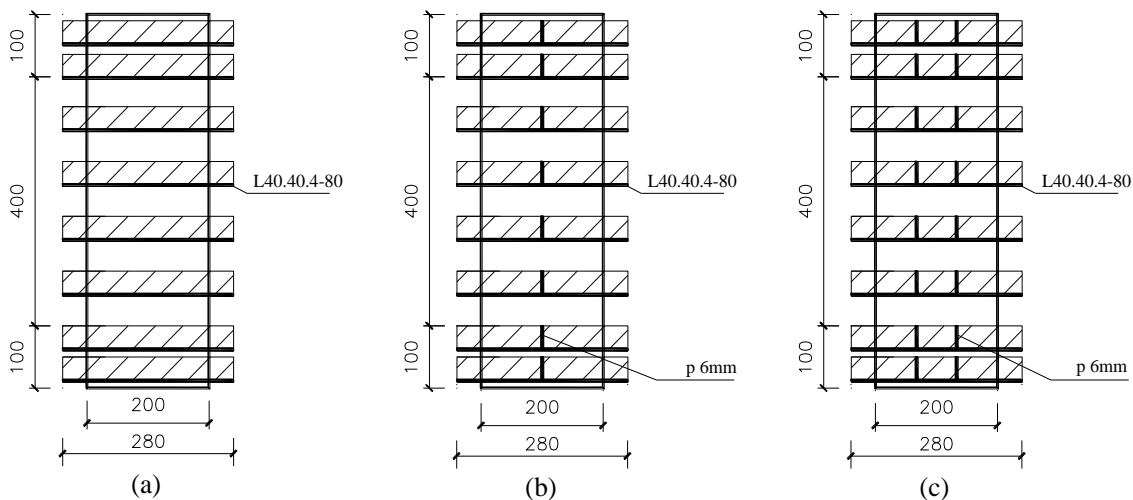


Fig. 3 – Elevation views of external confinement arrangements of specimens: (a) S04, S04a, S04b; (b) S04c; (c) S04d

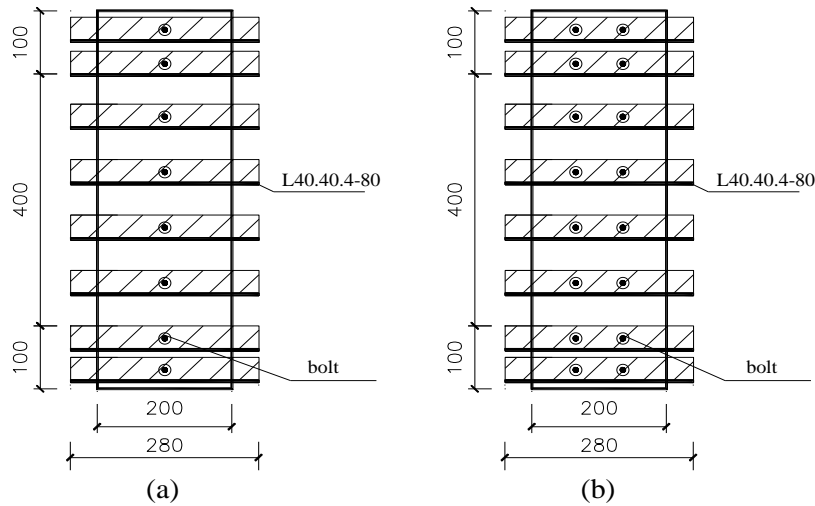


Fig. 4 – Elevation views of external confinement arrangements of specimens: (a) S04e; (b) S04f

in Figs. 5 and 6. Table 1 summarizes all the column specimens tested in the study.

Typical test setup of column specimens is shown in Fig. 7. The specimens are axially loaded with a displacement-controlled universal testing machine as shown in the figure. The machine is placed firmly on a strong floor to ensure no movement during the test. A Linear Variable Displacement Transducer (LVDT) is attached to each side of the column specimens for measuring the axial displacement during the test.

4. Discussions on test results

Standard concrete cylinders were made from the same mix proportion to obtain the mechanical properties of the concrete used in the specimens. The average compressive strength (f'_c) of the cylinders was 23.93 MPa with the standard deviation of 2.01 MPa. It was also found from the standard tensile test that the average yield strength (f_y) of the deformed bars was 317 MPa with the standard deviation of 5.9 MPa. The average tensile strength (f_u)

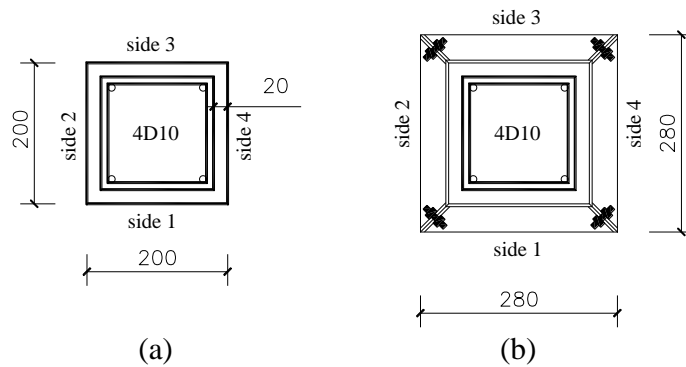


Fig. 5 – Cross sections of specimens: (a) CS01, CS03a; (b) S04, S04a, S04b

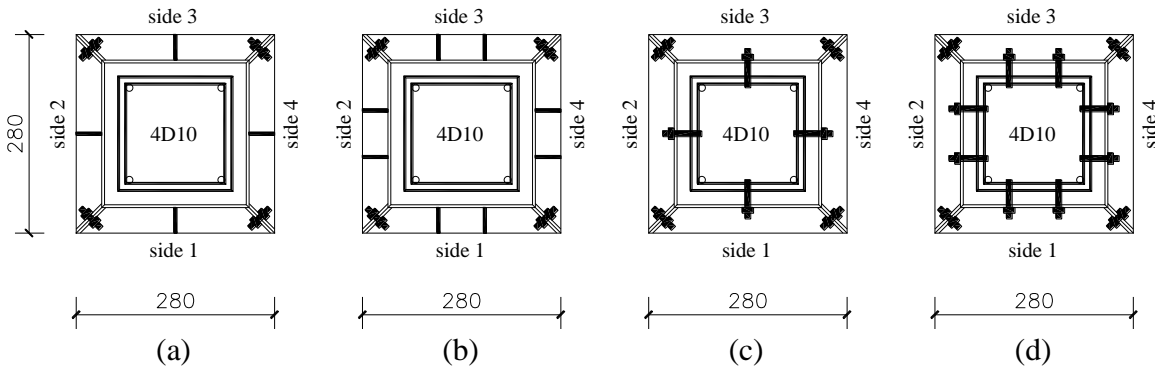


Fig. 6 – Cross sections of specimens: (a) S04c; (b) S04d; (c) S04e; (d) S04f

Table 1 – Details of column specimens

Column ID	Longitudinal bar	Confining steel	Stiffener/bolt
CS01	4-D10	None	None
CS03a	4-D10	D10-50 (vol. ratio = 2.36%)	None
S04	4-D10	L40.40.4-80 (vol. ratio = 9.60%)	None
S04a	4-D10	L40.40.4-80 (vol. ratio = 9.60%) D10-80 (vol. ratio = 1.48%) External confinement is placed exactly at the same location as internal confinement	None
S04b	4-D10	L40.40.4-80 (vol. ratio = 9.60%) D10-80 (vol. ratio = 1.48%) External confinement is placed at mid-spacing of internal confinement	None
S04c	4-D10	L40.40.4-80 (vol. ratio = 9.60%)	One stiffener
S04d	4-D10	L40.40.4-80 (vol. ratio = 9.60%)	Two stiffeners
S04e	4-D10	L40.40.4-80 (vol. ratio = 9.60%)	One bolt
S04f	4-D10	L40.40.4-80 (vol. ratio = 9.60%)	Two bolts

Note: All dimensions are in mm

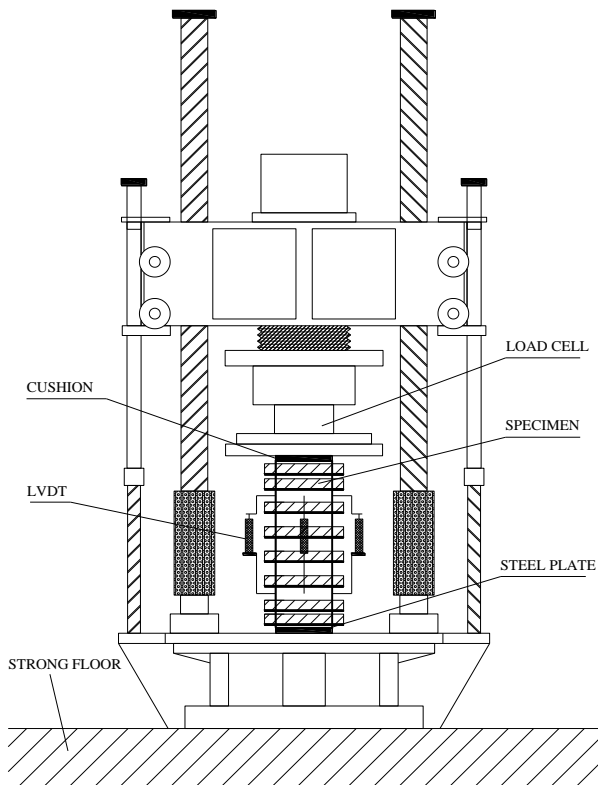


Fig. 7 – Typical test setup of column specimens

was 486 MPa with the standard deviation of 3.8 MPa. Three strip steel plates, cut from the L-shaped steel section, were also tested. The test indicated that the yield strength (f_{ySC}) of the L-shaped steel section was 285 MPa.

The stresses of the specimens (f_c) at any axial strains (ϵ_c) obtained from the test were normalized by the peak strength ($f'_{c0} = 19.07$ MPa) of unconfined Specimen CS01 in order to observe the

strength gain due to confinements. The normalized axial stress-strain curves of the specimens can be seen in Fig. 8. The enhancements of strength (f_c/f'_{c0}) and strain ductility (μ_s) are summarized in Table 2. In the study, the strain ductility, μ_s , is determined as the ratio of axial strain at 85 percent of peak stress in the descending (post-peak) branch (ϵ_{85}) of the strain-strain curve of confined concrete with respect to the strain at the peak stress ($\epsilon_{01} = 0.23$ percent) of unconfined concrete.

It can be seen that the unconfined Specimen CS01 showed non-ductile behavior. Seismically-confined Specimen CS03a indicated much better behavior in terms of strength and ductility enhancements. Specimen S04 did not perform as expected since one of the steel collars suffered a premature failure at its corner weld. The curve clearly indicated some strength gain, but relatively poor ductility.

Specimens S04c and S04d ($f_c/f'_{c0} = 1.25$ and 1.33, respectively) only showed slight strength improvement over Specimen S04 ($f_c/f'_{c0} = 1.21$). However, they (Specimens S04c and S04d) performed much higher ductilities ($\mu_s = 11.08$ and 10.47, respectively) compared to Specimen S04 ($\mu_s = 3.46$). It is important to note here that this ductility ratio does not represent the behavior of Specimen S04 as it is supposed to be. This is due to the premature failure of the collar's welds. It can be seen that the strengthening of the steel collars using web stiffeners was found to be ineffective. The confinement provided by the external steel collars primarily depends on the nominal axial and flexural capacities of the steel section [19]. Additional web stiffeners do not improve the capacities of the column, it only improves the local stability of steel

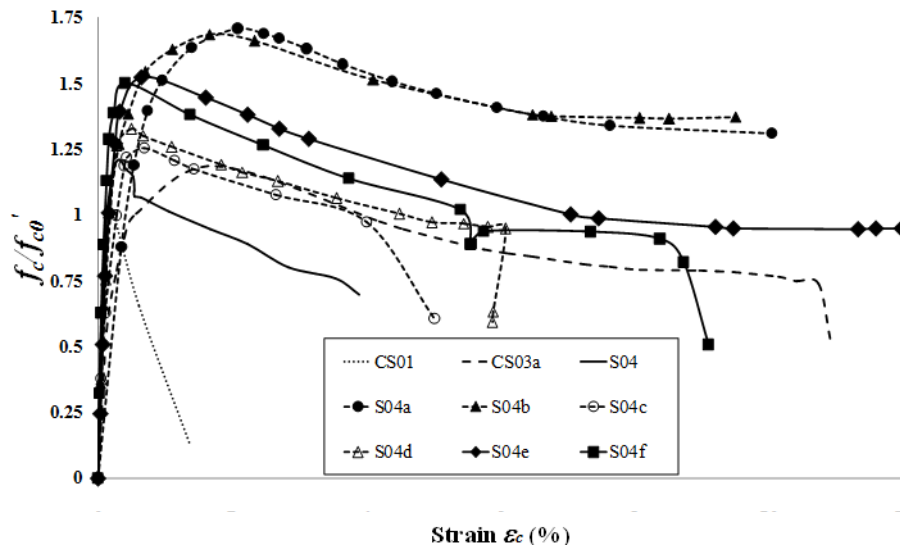


Fig. 8 – Normalized stress-strain curves

Table 2 – Enhancement of strengths and ductilities of the specimens

Column ID	f_c/f'_c0	μ_s
CS01	1.00	1.63
CS03a	1.19	15.55
S04	1.21	3.46
S04a	1.71	21.21
S04b	1.69	22.58
S04c	1.25	11.08
S04d	1.33	10.47
S04e	1.52	12.38
S04f	1.50	9.46

section from buckling which is not significant since the length of steel collar is relatively short.

Specimens S04e and S04f performed much better than Specimens S04c and S04d. The enhancements of strength (f_c/f'_c0) of Specimens S04e and S04f are found to be 1.52 and 1.50, respectively. However, in term of strain ductility, these specimens are comparable to Specimens S04c and S04d. Adding more bolts to better attach the steel collars is proven to be ineffective. In fact, Specimen S04f performed slightly inferior compared to Specimen S04e which used fewer bolts. This might be due to the fact that by using more bolts also means that more concrete damage could prematurely occur due to the drilling work.

Most importantly, Specimens S04a and S04b demonstrated the best results, which indicated that the proposed external confinement technique is very suitable for retrofitting purpose of existing RC columns. In Table 2, it can be clearly seen that both specimens showed much superior results than the remaining specimens. The strength of the speci-

mens improved up to 70 percent over the control Specimens CS01. The strain ductilities were also recorded very high ($\mu_s = 21.21$ and 22.58 for Specimens S04a and S04b, respectively).

Brittle diagonal splitting was observed in Specimen CS01, while intact confined concrete core was observed in Specimen CS03a (Fig. 9). It can be seen in Fig. 10 that the third collar in the test region (numbered bottom-up) of Specimen S04 suffered a corner failure due to the bulging concrete. Figures 11 and 12 illustrate the damages of Specimens S04a and S04b, respectively. Specimen S04b with closer combined spacing of internal and external confining steels suffered less overall damages. Figures 13 and 14 exhibit the damages of Specimens S04c and S04d, respectively. This set of specimens gained the least strength and ductility enhancements as compared to the standard-collared Specimen S04. Figures 15 and 16 depict the damages of Specimens S04e and S04f, respectively. Some bolts were detached from the concrete due to the excessive concrete core damages during testing.

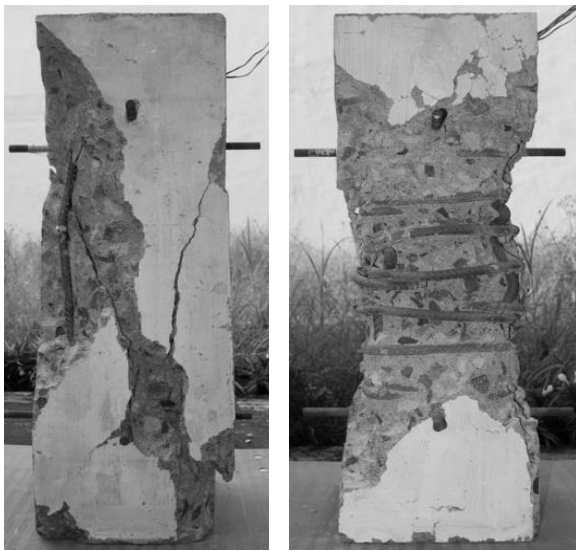


Fig. 9 – Specimens: (a) CS01; (b) CS03a, after completion of test

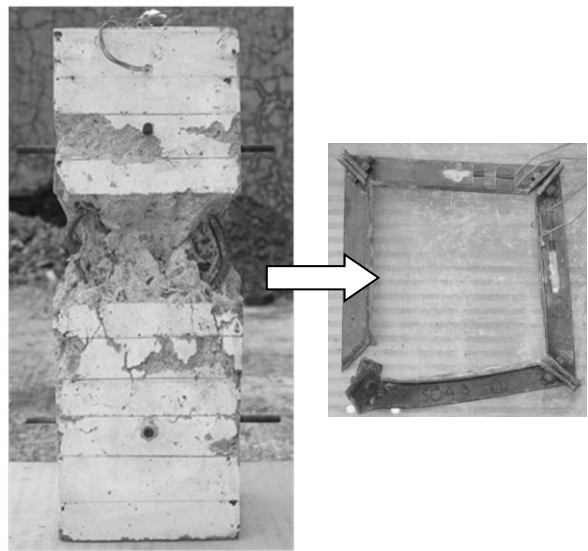


Fig. 10 – Specimen S04 after completion of test

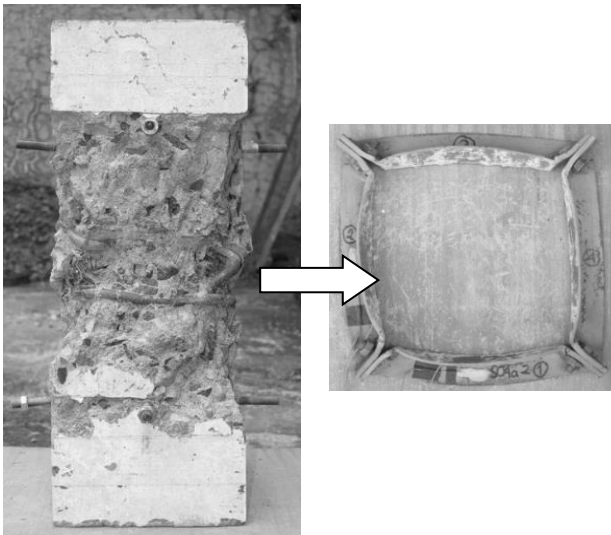


Fig. 11 – Specimen S04a after completion of test

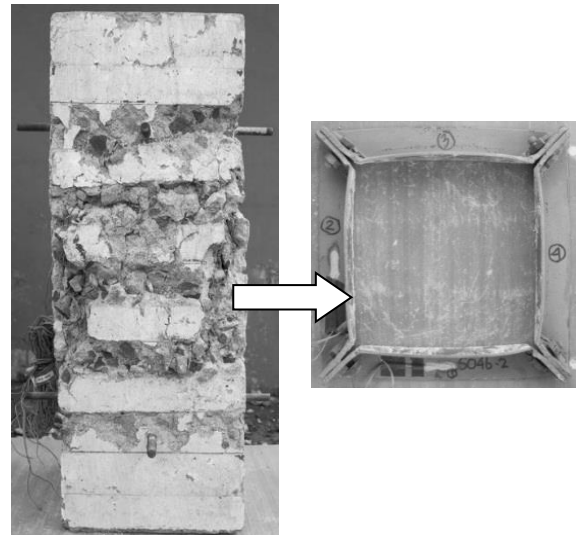


Fig. 12 – Specimen S04b after completion of test

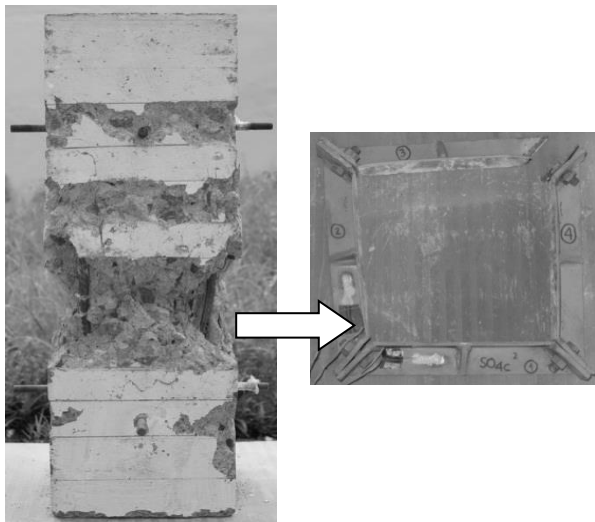


Fig. 13 – Specimen S04c after completion of test

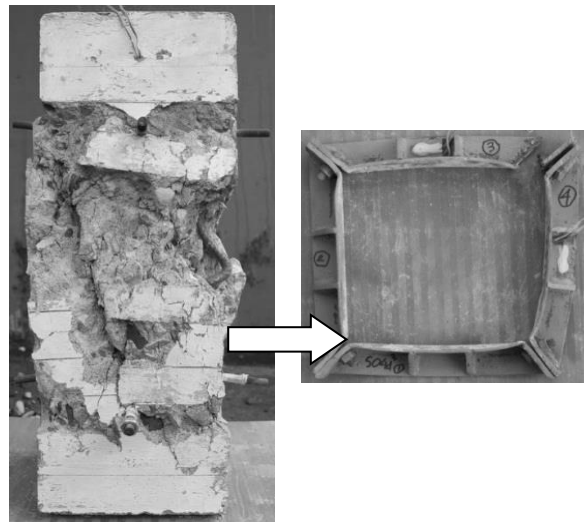


Fig. 14 – Specimen S04d after completion of test

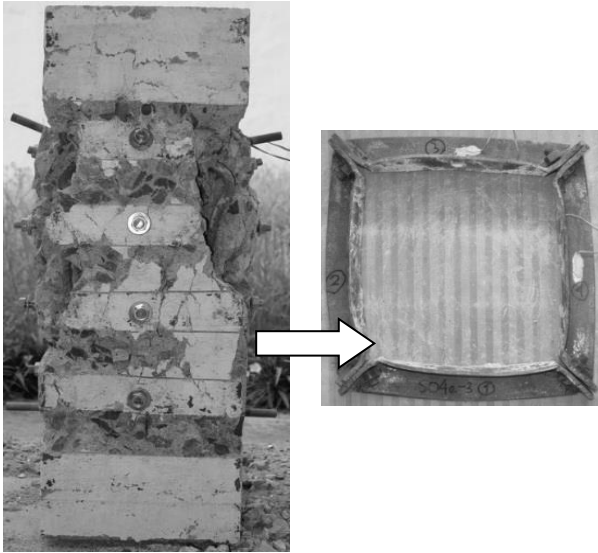


Fig. 15 – Specimen S04e after completion of test

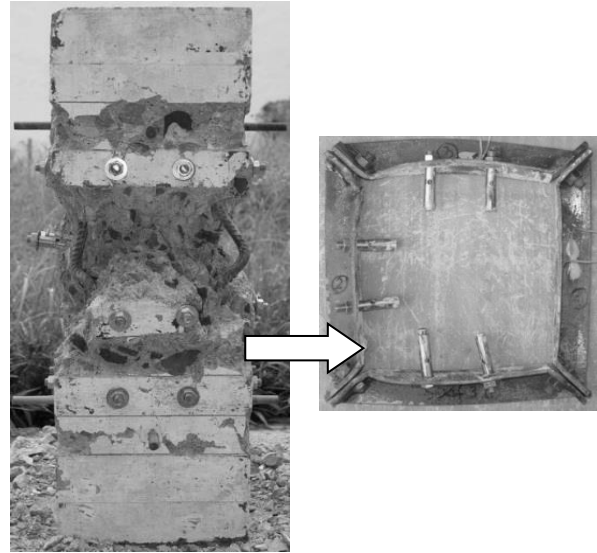


Fig. 16 – Specimen S04f after completion of test

5. Conclusions

An alternative of external confining technique for retrofitting square or rectangular concrete columns is presented. The technique has some promising advantages, such as better constructability (only minor cutting and welding processes are involved to prepare the steel collars), and higher applicability (the steel collars can be applied by only fastening the structural bolts at its four corners). Concentric static axial load tests have been conducted on nine column specimens to validate the reliability of the proposed technique. From the experimental program, some conclusions can be drawn as follows:

- (1) The introduction of external confinement using L-shaped steel collars has successfully enhanced both strength and ductility of RC columns. The compressive strength gain was observed as high as 21 percent for the standard-collared Specimen S04 compared with that without confinement. However, the ductility enhancement of Specimen S04 is not as good as expected due to the premature failure of collar's welds.
- (2) The control Specimen CS03a with the standard internal confinement required by the seismic provision showed 19 percent strength gain. All the L-shaped steel-collared specimens (except Specimen S04) showed higher strength gain than Specimen CS03a. Specimens S04c and S04d (steel collars with web stiffeners) showed the least strength improvement. Specimens S04e and S04f (steel collars with bolts) showed better strength improvement over Specimens S04c and S04d. Specimens with the combination of both internal stirrups and external steel collars (S04a and S04b) showed the

highest strength improvement than the remaining specimens.

- (3) In terms of ductility, control Specimen CS03a gave the strain ductility ratio of 15.55. Specimens retrofitted only with L-shaped steel collars (S04c, S04d, S04e, and S04f) indicated slightly less ductility than Specimen CS03a despite their excellent strength gains. Only Specimens S04a and S04b performed better ductility than Specimen CS03a.
- (4) The retrofit of existing RC columns simulated by Specimens S04a and S04b has demonstrated excellent results. These set of specimens exhibited the best performance with strength gain found as high as 71 percent. Both tests were terminated due to the limitation of LVDT's capacity. Both specimens can still maintain at least 78 percent of their peak load carrying capacities

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